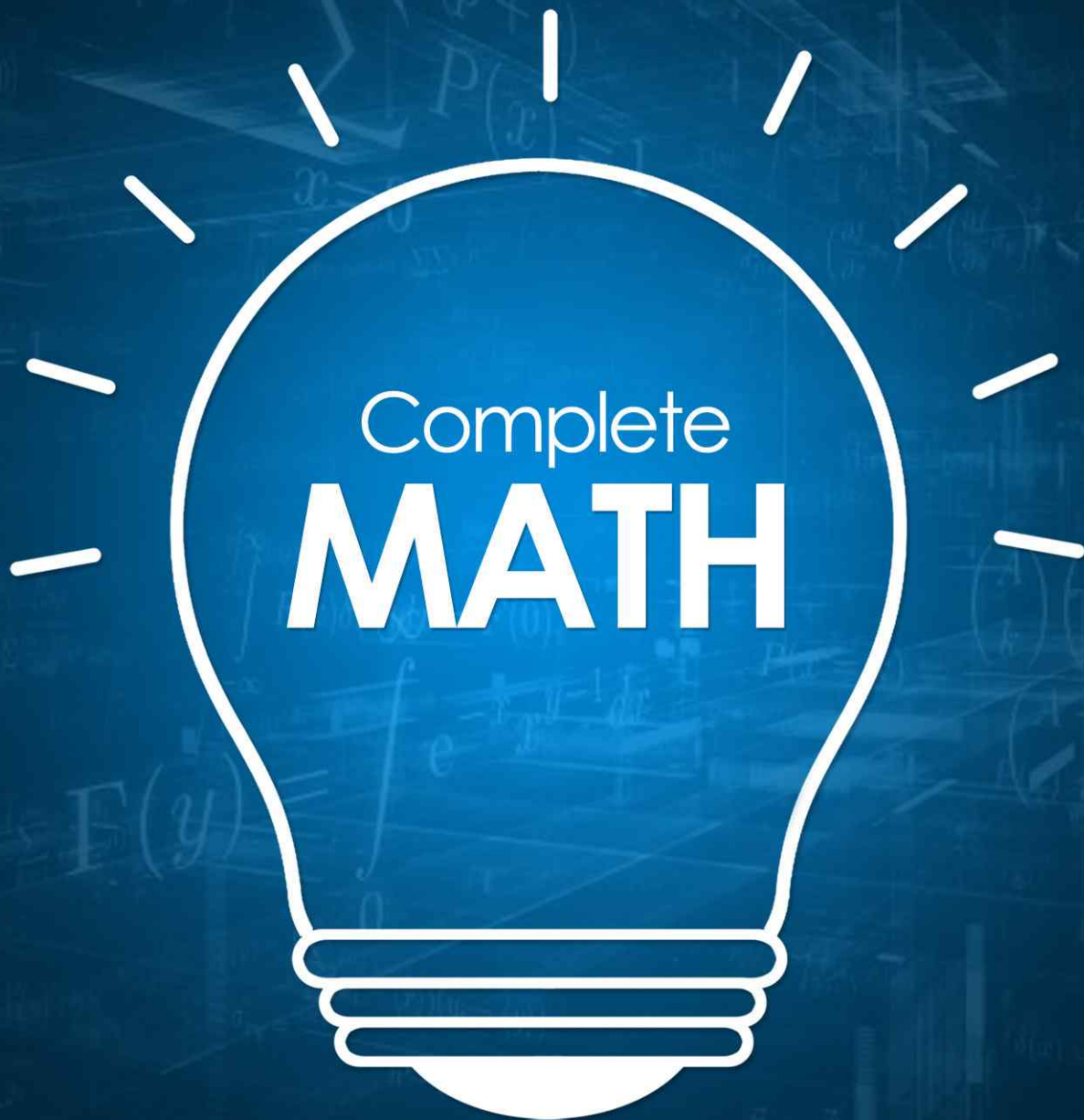




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CLASS 11th

Limits And Derivatives

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We can approach to a given number 'a' (say) on the real line either from its left hand side by increasing numbers which are less than 'a' or from right hand side by decreasing numbers which are greater than 'a'. So, there are two types of limits viz. (i) left hand limit and (ii) right hand limit. For some functions at a given point 'a' (say) left and right hand limits are equal whereas for some functions these two limits are not equal and even sometimes either left hand limit or right hand limit or both do not exist.

If $\lim_{x \rightarrow a^-} f(x) = \lim_{x \rightarrow a^+} f(x)$ i.e., (LHL at $x = a$) = (RHL at $x = a$),

then we say that $\lim_{x \rightarrow a} f(x)$ exists. Otherwise, $\lim_{x \rightarrow a} f(x)$ does not exist.

01. Evaluation of Left Hand and Right Hand Limits

$x \rightarrow a^-$ means that x is tending to a from that left hand side, i.e., x is a number less than a but very close to a . Therefore, $x \rightarrow a^-$ is equivalent to $x = a - h$ where $h > 0$ such that $h \rightarrow 0$.

Similarly, $x \rightarrow a^+$ is equivalent to $x = a + h$ where $h \rightarrow 0$.

(A) We have the following algorithm for finding left hand limit at $x = a$.

Algorithm

- STEP I Write $\lim_{x \rightarrow a^-} f(x)$
- STEP II Put $x = a - h$ and replace $x \rightarrow a^-$ by $h \rightarrow 0$ to obtain $\lim_{h \rightarrow 0} f(a - h)$.
- STEP III Simplify $\lim_{h \rightarrow 0} f(a - h)$ by using the formula for the given function.
- STEP IV The value obtain in step III is the LHL of $f(x)$ at $x = a$.

(B) To evaluate RHL of $f(x)$ at $x = a$ i.e. $\lim_{x \rightarrow a^+} f(x)$ we use the following algorithm.

Algorithm

- STEP I Write $\lim_{x \rightarrow a^+} f(x)$
- STEP II Put $x = a + h$ and replace $x \rightarrow a^+$ by $h \rightarrow 0$ to obtain $\lim_{h \rightarrow 0} f(a + h)$.
- STEP III Simplify $\lim_{h \rightarrow 0} f(a + h)$ by using the formula for the given function.
- STEP IV The value obtain in step III is the RHL of $f(x)$ at $x = a$.

REMARK If f is an odd function and if $\lim_{x \rightarrow 0} f(x)$ exists. Prove that this limit must be zero.