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CLASS 11&12th



CLASS 12th

Electrostatics-II



01. Introduction

(i) When a conductor is given a charge, it's potential rises in proportional to the charge given i. e.

$$Q \propto V$$
 or $Q = CV$ or $C = Q/V$

This C is a constant and is called the CAPACITANCE of conductor

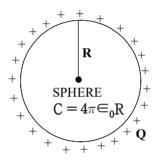
- (ii) A given conductor can be charged to a limit. Charging after the limit results into ionization of medium, and charge gets leaked into medium
- (iii) C depends on
 - (1) Size and shape of conductor
 - (2) Surrounding medium
 - (3) Presence of other conductor near by
- (iv) Unit (1) Coulomb/volt
 - (2) Farad
 - 1 Farad = 1 Coulomb/volt.

Capacitance of an isolated spherical conductor

Q: Charge on the sphere

V: Potential at the surface of sphere

R: Radius of sphere



(i)
$$V = \frac{Q}{4\pi\epsilon_0 R}$$
 also $V = \frac{Q}{C}$

hence
$$C = 4\pi\varepsilon_0 R$$

02. Energy of a Charged Conductor

- (i) The work done in charging the conductor gets stored as potential energy in the electric field in the vicinity of the conductor.
- (ii) Suppose, a conductor is given a charge q, then potential of conductor $V = \frac{q}{C}$

Work done to bring a further charge dq is given by $d_W = V dq = \frac{q}{C} dq$

So, work done to charge it from 0 to Q is

$$W = \frac{1}{C} \int_{0}^{Q} q \, dq = \frac{Q^{2}}{2C} = \frac{1}{2} CV^{2} = \frac{1}{2} QV.$$

This is energy U which is stored.

(iii) This energy does not depend upon size of the conductor

03. Distribution of Charges

- (i) Two insulated conductors A and B of capacitances C_1 and C_2 are given charges q_1 and q_2 and raised to potential V_1 and V_2 respectively. Then $q_1 = C_1 V_1$ and $q_2 = C_2 V_2$
- (ii) When, these conductors are joined by a thin wire, then positive charge will flow from the conductor at higher charge will flow from the conductor at higher potential to conductor at lower potential till their potentials become equal.
- (iii) Charge remains conserved in this process i.e. If q'₁ and q'₂ are charges after distribution and V the potential on each conductor then

$$\begin{aligned} &\mathbf{q'}_1 = \mathbf{C}_1 \mathbf{V} \\ \text{and} &\ &\mathbf{q'}_2 = \mathbf{C}_2 \mathbf{V} \\ \text{and} &\ &\mathbf{C}_1 \mathbf{V}_1 + \mathbf{C}_2 \mathbf{V}_2 = \mathbf{C}_1 \mathbf{V} + \mathbf{C}_2 \mathbf{V} \end{aligned}$$

(iv)
$$V = \frac{\text{Total charge}}{\text{Total } \cap \text{acitance}} = \frac{C_1 V_1 + C_2 V_2}{C_1 + C_2}$$

(v) On connecting two charged conductors their distributed charged on them are in the ratio of their capacitances

i.e.
$$\frac{q_1}{q_2} = \frac{C_1}{C_2}$$

(vi) Loss of energy:

$$\Delta U = U_{\text{initial}} - U_{\text{final}}$$
$$\Delta U = \frac{1}{2} \frac{C_1 C_2}{C_1 + C_2} (V_1 - V_2)^2$$

04. Capacitor/Condenser